

NAME.....

Intuitive Calculus 11012 Quiz A

April 8, 2010 Richard M. Aron

1. Find each indefinite integral:

$$(a). \int 18y^{17} dy = y^{18} + C$$

$$(b). \int (u+1)(u+2) du = \int (u^2 + 3u + 2) du \\ = \frac{u^3}{3} + \frac{3u^2}{2} + 2u + C$$

$$(c). \int (e^{3x} - \frac{3}{x}) dx = \frac{e^{3x}}{3} - 3 \ln x + C$$

2. The cost of maintaining a home generally increases as the home becomes older. Suppose that the rate of cost (dollars per year) for a home that is  $x$  years old is  $200e^{0.4x}$ . Find a formula for the total maintenance cost during the first  $x$  years. (Maintenance should be zero at  $x = 0$ .)

Given  $r(t) = 200e^{.4x}$ . So,  $M(t) =$  maintenance cost =  $\int r(t) dt = 500 \cdot e^{.4x} + C$ . Now, in the beginning, when  $x=0$ ,  $M(0) = 0$ . So,  $0 = 500e^0 + C = 500 + C$ . Get  $C = -500$ . Thus,  $M(t) = 500e^{.4x} - 500$ . (So, eg, after 5 years one is spending over \$3000 for maintenance)

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Intuitive Calculus 11012 Quiz B

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1. Find each indefinite integral:

$$(a). \int 10u^9 du = u^{10} + C$$

$$(b). \int (x-1)(x+2) dx = \int (x^2 + x - 2) dx \\ = \frac{x^3}{3} + \frac{x^2}{2} - 2x + C$$

$$(c). \int (e^{2x} - \frac{2}{x}) dx = \frac{e^{2x}}{2} - 2 \ln x + C$$

2. An ice cube tray filled with tap water is placed in the freezer, and the temperature of the water is changing at the rate of  $-12e^{-0.2t}$  degrees per hour after  $t$  hours. The original temperature of the tap water was 70 degrees. Find a formula for the temperature of water that has been in the freezer for  $t$  hours.

Given:  $r(t) = -12e^{-.2t}$ , Temperature  $T(t) = \int r(t) dt = 60e^{-.2t} + C$ . Now, at time  $t=0$ ,  $T(0) = \text{original temperature} = 70 = 60e^0 + C$ . So,  $C = 10$ . Thus,  $T(t) = 60e^{-.2t} + 10$ . (So, after 5 hours, the water should be frozen).