

Name: _____ Quiz Score: _____ /20

Quiz 5: Monday, November 17, 2014

For each of the following:

- sketch a timeline with all (possible) payments, their discounts, and probabilities;
- give a formula (any); and
- explain what it represents in plain English. Your explanations should make the difference between the symbols clear.

1. $\ddot{a}_{\overline{n}|d}$ = the present value of an annuity that pays \$1 per year ^(annually) at the beginning of each year for n payments.

| | | | | | | | | | | |
|-----------------|-----|-----|----------------|--|--|--|--|------------------|------------------|----------------|
| time (years) | 0 | 1 | 2 | | | | | n-2 | n-1 | n |
| payment | \$1 | \$1 | \$1 | | | | | -\$1 | \$1 | |
| discount factor | 1 | v | v ² | | | | | v ⁿ⁻² | v ⁿ⁻¹ | v ⁿ |

TS

2. $A_x = \sum_{k=0}^{\infty} v^{k+1} (p_x)^k (q_x) =$ expected present value of a single \$1 payment at the end of the year that a life aged x dies in

| | | | | | | | | | | | |
|-------------------------|---|-------|---------------------|--|--|--|--|-----------------------------|-----------------------------|-----------------------|-----|
| time (years) from age x | 0 | 1 | 2 | | | | | n-1 | n | n+1 | |
| possible payments | ⊛ | \$1 | \$1 | | | | | TS | \$1 | \$1 | \$1 |
| discount factor | | v | v ² | | | | | v ⁿ⁻¹ | v ⁿ | v ⁿ⁺¹ | |
| probability | | q_x | $p_x \cdot q_{x+1}$ | | | | | $p_x^{n-2} \cdot q_{x+n-2}$ | $p_x^{n-1} \cdot q_{x+n-1}$ | $p_x^n \cdot q_{x+n}$ | |

continued on the reverse

⊛ only get one payment, depending on the year that the life aged x dies in (if (x) dies in the year x+2.5, then the \$1 payment is made at the end of the year x+3)

