Names: $\qquad$ .

## Fair Division Worksheet

1. A round pizza is half cheese and half pepperoni. It costs $\$ 7.20$. Walter values pepperoni four times as much as cheese. Jesse values cheese twice as much as pepperoni.
(a) Find the value of the cheese half of the pizza, according to Walter's value system. Round to the nearest cent.
(b) Find the value of the pepperoni half of the pizza, according to Walter's value system. Round to the nearest cent.
(c) Find the value of a $45^{\circ}$ cheese slice of pizza, according to Walter's value system. Round to the nearest cent.
(d) Find the value of a $60^{\circ}$ pepperoni slice of pizza, according to Walter's value system. Round to the nearest cent.
(e) Find the value of the cheese half of the pizza, according to Jesse's value system. Round to the nearest cent.
(f) Find the value of the pepperoni half of the pizza, according to Jesse's value system. Round to the nearest cent.
(g) Find the value of a $45^{\circ}$ cheese slice of pizza, according to Jesse's value system. Round to the nearest cent.
(h) Find the value of a $60^{\circ}$ pepperoni slice of pizza, according to Jesse's value system. Round to the nearest cent.
2. Six friends agree to divide a $\$ 18$ pizza fairly using the Lone Divider Method. The table shows how each player values each of the six slices that have been cut by the divider. Assume that all of the friends play honestly.

|  | $s_{1}$ | $s_{2}$ | $s_{3}$ | $s_{4}$ | $s_{5}$ | $s_{6}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tuco | $\$ 1$ | $\$ 2$ | $\$ 1$ | $\$ 1$ | $\$ 1$ | $\$ 13$ |
| Hector | $\$ 3$ | $\$ 3$ | $\$ 3$ | $\$ 3$ | $\$ 3$ | $\$ 3$ |
| Leonel | $\$ 8$ | $\$ 2$ | $\$ 2$ | $\$ 2$ | $\$ 2$ | $\$ 2$ |
| Marco | $\$ 5$ | $\$ 2$ | $\$ 3$ | $\$ 2$ | $\$ 2$ | $\$ 4$ |
| Tortuga | $\$ 2$ | $\$ 2$ | $\$ 8$ | $\$ 1$ | $\$ 3$ | $\$ 2$ |
| Don Eliado | $\$ 10$ | $\$ 1$ | $\$ 0$ | $\$ 4$ | $\$ 0$ | $\$ 3$ |

(a) How much is a fair share worth?
(b) Which player was the Divider?
(c) Give the bid list (declaration) for each player.

| player | Tuco | Hector | Leonel | Marco | Tortuga | Don Eliado |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| bid list |  |  |  |  |  |  |

(d) Give a possible Fair Division of the pizza, if one exists.

| player | Tuco | Hector | Leonel | Marco | Tortuga | Don Eliado |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| slice received |  |  |  |  |  |  |

(e) What would the players do if there were no possible fair division of these slices?
3. Three students, Andrea, Brock, and Combo, divide fairly 20 pieces of candy, of different types, using the Method of Markers. The candy is placed in an array and the players bid by placing markers as shown below. (Marker $A_{1}$ is Andrea's first marker, $A_{2}$ is her second; $B_{1}$ and $B_{2}$ are Brock's markers, and $C_{1}$ and $C_{2}$ are Combo's.) It is agreed that candy leftover after the allocation will be put aside for a rainy day Recall that our convention is to go from left to right.


Which pieces does each person get?

| player | Andrea | Brock | Combo | Leftovers |
| :---: | :---: | :---: | :---: | :---: |
| pieces received |  |  |  |  |

4. Four heirs, Skyler, Flynn, Holly, and Marie divide fairly an estate consisting of four items- a car wash, a house, a car, and a watch- using the Method of Sealed Bids. The players' bids are given in the table below.
(a) (The Bids) Determine each player's opinion of the total value of the estate and the value that each player places on a fair share. Enter these values in rows (1) and (2) of the table.
(b) (The Allocation) Determine the allocation of the items in the estate. Fill in the item(s) allocated to each player in row (3) of the table.
(c) (The Payments) After the items are allocated, some players will owe the estate money and others will be owed money by the estate. Determine the amount of money each player owes or is owed and enter this in row (4) $O R$ (5) of the table.
(d) (Dividing the Surplus) After the payments are all made, there might be a surplus left in the estate. Determine each player's share of the surplus and enter it in row (6) of the table.
(e) (Final Settlement) Find the net settlement (items and money) for each player and enter it in row (7) of the table.

|  |  |  | Skyler | Flynn | Holly | Marie |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bids |  | Car Wash | \$800,000 | \$500,000 | \$750,000 | \$100,000 |
|  |  | House | \$200,000 | \$120,000 | \$250,000 | \$180,000 |
|  |  | Car | \$10,000 | \$9,000 | \$6,000 | \$5,000 |
|  |  | Watch | \$1,000 | \$1,500 | \$1,200 | \$1100 |
|  |  | Total Value of Estate |  |  |  |  |
|  | (2) | Value of a Fair Share |  |  |  |  |
| Allocation | (3) | Item(s) Allocated |  |  |  |  |
| Payments | (4) | Player Owes Estate |  |  |  |  |
|  | (5) | Estate Owes Player |  |  |  |  |
| Surplus | (6) | Share of Surplus |  |  |  |  |
| Final Settlement |  | Final Settlement <br> Items: <br> Money (+/-): |  |  |  |  |

5. Saul and Huell buy a 12 -inch half-ham, half-turkey sub sandwich for $\$ 4.80$. (So there are 6 inches of ham and 6 inches of turkey.) Saul values turkey three times as much as ham. Huell values ham five times as much as turkey.
(a) Find the value of 1 inch of ham and 1 inch of turkey to Saul.
(b) Find the value of 1 inch of ham and 1 inch of turkey to Huell.
(c) If Saul were the divider in a two-person Divider-Chooser game, where would he cut the sandwich? (Suppose he must make just one cut, cross-wise.)
(d) How much would each of the pieces Saul cut be worth to Huell?
(e) If Huell were the divider in a two-person Divider-Chooser game, where would he cut the sandwich? (Suppose he must make just one cut, cross-wise.)
(f) How much would each of the pieces Huell cut be worth to Saul?
