

“Area-So-Far Functions”

1. Let f be the constant function $f(x) = 5$.

- (a) Sketch the graph of f on a sheet of graph paper.
 (b) Define the “area-so-far” function A by $A(x)$ is the area under the graph $y = f(x)$ from 0 to x . Compute each of the following using geometric formulas.

- | | |
|------------|-------------|
| i. $A(0)$ | iii. $A(2)$ |
| ii. $A(1)$ | iv. $A(3)$ |

(c) Find a formula for $A(x)$. Sketch the appropriate rectangle on the graph of f . Label the lengths of its sides.

(d) Define another “area-so-far” function F by $F(x)$ is the area under the graph $y = f(x)$ from -1 to x . Compute each of the following using geometric formulas.

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|------------|-------------|
| i. $F(0)$ | iii. $F(2)$ |
| ii. $F(1)$ | iv. $F(3)$ |

(e) Find a formula for $F(x)$. Sketch the appropriate rectangle on the graph of f . Label the lengths of its sides.

2. Let f be the function $f(x) = 2x$.

- (a) Sketch the graph of f on a sheet of graph paper.
 (b) Define the “area-so-far” function A by $A(x)$ is the area under the graph $y = f(x)$ from 0 to x . Compute each of the following using geometric formulas.

- | | |
|------------|-------------|
| i. $A(0)$ | iii. $A(2)$ |
| ii. $A(1)$ | iv. $A(3)$ |

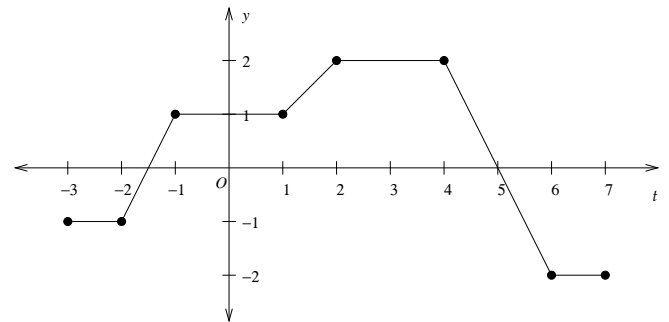
(c) Find a formula for $A(x)$. Sketch the appropriate geometric figure on the graph of f .

(d) Define another “area-so-far” function F by $F(x)$ is the area under the graph $y = f(x)$ from 1 to x . Compute each of the following using geometric formulas.

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|------------|-------------|
| i. $F(1)$ | iii. $F(3)$ |
| ii. $F(2)$ | iv. $F(4)$ |

(e) Find a formula for $F(x)$. Sketch the appropriate geometric figure on the graph of f .

3. Consider the function f whose graph is given.



(a) Define the “area-so-far” function A by $A(x)$ is the area under the graph $y = f(x)$ from 0 to x . Compute each of the following using geometric formulas.

- | | |
|-------------|------------|
| i. $A(0)$ | iv. $A(3)$ |
| ii. $A(1)$ | v. $A(4)$ |
| iii. $A(2)$ | vi. $A(5)$ |

(b) Define another “area-so-far” function F by $F(x)$ is the area under the graph $y = f(x)$ from -1 to x . Compute each of the following using geometric formulas.

- | | |
|-------------|-------------|
| i. $F(-1)$ | v. $F(3)$ |
| ii. $F(0)$ | vi. $F(4)$ |
| iii. $F(1)$ | vii. $F(5)$ |
| iv. $F(2)$ | |