

Name: \_\_\_\_\_ Score: \_\_\_\_\_ /100  
(113 pts available)

**EXAM 3: Version B**

NO CALCULATORS.

**Multiple Choice: 17 questions at 4 points each.**

*Circle the letter of the best response.*

*Although your work will not be graded, you should write out complete and careful solutions to reduce the chance of error.*

1. The lowest point of the graph of  $f(x) = x^3 - 3x + 1$  on the interval  $[-1, 3]$  is

- (a)  $(1, -1)$
- (b)  $(-1, 0)$
- (c)  $(2, -9)$
- (d)  $(0, -3)$
- (e) none of these

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2. The highest point of the graph of  $f(x) = x^3 - 3x + 1$  on the interval  $[-1, 3]$  is

- (a)  $(3, 24)$
- (b)  $(0, 1)$
- (c)  $(-1, 3)$
- (d)  $(3, 19)$
- (e) none of these

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3. True or False: Suppose  $f$  is continuous and that  $f'(7) = 0$  and  $f''(7) = -10$ . Then we may conclude that  $f$  has an **absolute maximum** point at  $x = 7$ .

- (a) True
- (b) False

4. True or False: If  $f$  is continuous on the interval  $[1, 5]$ , then  $f$  must have an **absolute minimum value** on  $[1, 5]$ .

- (a) True
  - (b) False
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5. True or False: If  $f$  is continuous on the interval  $(1, 5)$ , then  $f$  must have an **absolute minimum value** on  $(1, 5)$ .

- (a) True
  - (b) False
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6. An automobile dealer can sell 8 cars per day at a price of \$25,000. He estimates that for each \$1000 price reduction, he can sell 3 more cars each day. Let  $x$  be the number of \$1000 price reductions. Find an expression for the price per car (in dollars).

- (a)  $25,000 \times 1000x$
  - (b)  $25,000 - 8x$
  - (c)  $25,000 - 1000x$
  - (d)  $25,000x - 1000$
  - (e) none of these
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7. An automobile dealer can sell 8 cars per day at a price of \$25,000. He estimates that for each \$1000 price reduction, he can sell 3 more cars each day. Let  $x$  be the number of \$1000 price reductions. Find an expression for the number of cars sold per day.

- (a)  $8 - 1000x$
  - (b)  $8x$
  - (c)  $8 - 3x$
  - (d)  $8 + 3x$
  - (e) none of these
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8. If the reproduction function for Albacore tuna is  $f(p) = 5\sqrt[3]{p^2}$  (where both  $p$  and  $f(p)$  are in thousands), find the sustainable yield for a population of 8000 tuna. (Evaluate  $Y(8)$  where  $Y(p)$  is the sustainable yield function.)

- (a) 8,000 tuna
  - (b) 12,000 tuna
  - (c) 16,000 tuna
  - (d) 20,000 tuna
  - (e) none of these
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9. Evaluate the integral:  $\int 2.4x \, dx$

- (a)  $2.4 + C$
- (b)  $2.4x^2 + C$
- (c)  $4.8x^2 + C$
- (d)  $1.2x^2 + C$
- (e) none of these

10. Evaluate the integral:  $\int \frac{5}{x^4} dx$

- (a)  $5 \ln |x^4| + C$
  - (b)  $\frac{1}{x^5} + C$
  - (c)  $-\frac{15}{x^3} + C$
  - (d)  $-\frac{5}{3x^3} + C$
  - (e) none of these
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11. Evaluate the integral:  $\int 8e^{2t} dt$

- (a)  $8e^{2t} + C$
  - (b)  $16e^{2t} + C$
  - (c)  $4e^{2t} + C$
  - (d)  $16e^{3t} + C$
  - (e) none of these
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12. Evaluate the integral:  $\int \frac{6x^2 - 4x + 7}{x^2} dx$

- (a)  $\frac{2x^3 - 2x^2 + 7x}{\frac{1}{3}x^3} + C$
  - (b)  $6x - 4 \ln |x| - \frac{7}{x} + C$
  - (c)  $6x - 4 \ln |x| - \frac{7}{3x^3} + C$
  - (d)  $6x - 4 \ln |x| - \frac{21}{x^3} + C$
  - (e) none of these
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13. Black squirrel flu is spreading on campus at a rate of  $10e^{0.5t}$  new cases per day, where  $t$  is the number of days since the start of the epidemic. The epidemic began with 1 case. Find an expression for the total number of flu cases during the first  $t$  days.

- (a)  $20e^{0.5t} - 19$
- (b)  $20e^{0.5t} + 1$
- (c)  $10e^{0.5t} + 1$
- (d)  $5e^{0.5t}$
- (e) none of these

14. Evaluate the integral:  $\int_e^{e^4} \frac{10}{x} dx$ .

- (a)  $e^3$
  - (b) 0
  - (c) 3
  - (d) 30
  - (e) none of these
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15. Find the area under the curve  $y = x^2 + 4x$  from  $x = 0$  to  $x = 2$ .

- (a)  $\frac{32}{3}$
  - (b)  $\frac{20}{3}$
  - (c)  $\frac{44}{3}$
  - (d) 12
  - (e) none of these
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16. A company is considering a new manufacturing process. The rate of savings from this process is expected to be  $\frac{12,000}{t^2}$  dollars per year, where  $t$  is in years. Determine the total savings from the third through the sixth year.

- (a) \$2000
  - (b) \$4000
  - (c) \$8000
  - (d) \$12,000
  - (e) none of these
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17. Complete the statement of The Fundamental Theorem of Calculus.

Let  $f$  be continuous on  $[a, b]$ . Then  $\int_a^b f(x) dx =$

- (a)  $f(b) - f(a)$
- (b)  $f'(b) - f'(a)$
- (c)  $F(a) - F(b)$ , where  $F$  is any antiderivative of  $f$ .
- (d)  $F(b) - F(a)$ , where  $F$  is any antiderivative of  $f$ .
- (e) none of these

### Long Answer

Write all work carefully and neatly for full credit.

18. (25 points) A company wants to build a rectangular parking lot along the side of a building using 200 yards of fence. The side along the building needs no fence. What are the dimensions of the largest such parking lot?
- (a) (3 pts) Draw three different possible parking lots.
- (b) (4 pts) Introduce your variables with “Let” statements. (Include the units.)
- (c) (2 pts) Express the area  $A$  of the parking lot in terms of your variables.
- (d) (3 pts) Write a constraint equation relating your variables. (*Skip this step if you have only one variable.*)
- (e) (2 pts) Express the area  $A$  in terms of one variable only.
- (f) (5 pts) Use calculus to find the value of the variable for which  $A$  is maximal.
- (g) (4 pts) Verify that you have indeed found the **absolute maximum** point of  $A$  (on an appropriate interval, if necessary).
- (h) (2 pts) Answer the question in a complete sentence.

19. (20 points) Evaluate each integral, simplifying your answer and writing out all work, including substitutions, if any. Be sure to use correct notation.

(a)  $\int \sqrt{x^6 + 9} x^5 dx$

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(b)  $\int_{-2}^4 \frac{1}{5-x} dx$