

Instructions: Verify the following identities.

1. $\frac{\sin^2 \theta + \cos^2 \theta}{\cos^2 \theta \sec^2 \theta} = 1$

2. $2 \csc^2 \beta = \frac{1}{1 - \cos \beta} + \frac{1}{1 + \cos \beta}$

3. $\frac{\sec^2 \theta - 1}{\sec^2 \theta} = \sin^2 \theta$

4. $(\sec^2 x - 1)(\sin^2 x - 1) = -\sin^2 x$

5. $\csc x - \sin x = \cos x \cot x$

6. $\csc(x) + \cot(x) = \frac{\sin(x)}{1 - \cos(x)}$

7. $\frac{\tan^2 \theta}{1 + \sec \theta} = \frac{1 - \cos \theta}{\cos \theta}$

8. $\tan^3 x = \tan x \sec^2 x - \tan x$

9. $\sin^3 x \cos^4 x = (\cos^4 x - \cos^6 x) \sin x$

10. $\sqrt{\frac{1 + \sin \theta}{1 - \sin \theta}} = \frac{1 + \sin \theta}{|\cos \theta|}$