

**MATH 12002**  
**Assignment #27**  
**Derivatives**

The following are the derivatives for the problems in Assignment #27 on §3.4. You *are* expected to compute the derivatives yourself on the homework, but these can be used to check your answers before graphing.

$$\begin{aligned}4. \quad f(x) &= 8x^2 - x^4 = x^2(2\sqrt{2} - x)(2\sqrt{2} + x) \\ f'(x) &= 16x - 4x^3 = 4x(2 - x)(2 + x) \\ f''(x) &= 16 - 12x^2 = 12\left(\frac{2}{\sqrt{3}} - x\right)\left(\frac{2}{\sqrt{3}} + x\right)\end{aligned}$$

$$\begin{aligned}10. \quad f(x) &= \frac{x}{(x-1)^2} \\ f'(x) &= -\frac{x+1}{(x-1)^3} \\ f''(x) &= \frac{2(x+2)}{(x-1)^4}\end{aligned}$$

$$\begin{aligned}11. \quad f(x) &= \frac{1}{x^2 - 9} = \frac{1}{(x-3)(x+3)} \\ f'(x) &= -\frac{2x}{(x^2 - 9)^2} = -\frac{2x}{(x-3)^2(x+3)^2} \\ f''(x) &= \frac{6x^2 + 18}{(x^2 - 9)^3} = \frac{6x^2 + 18}{(x-3)^3(x+3)^3}\end{aligned}$$

$$\begin{aligned}13. \quad f(x) &= \frac{x}{x^2 + 9} \\ f'(x) &= \frac{9 - x^2}{(x^2 + 9)^2} = \frac{(3-x)(3+x)}{(x^2 + 9)^2} \\ f''(x) &= \frac{2x(x^2 - 27)}{(x^2 + 9)^3} = \frac{2x(x - 3\sqrt{3})(x + 3\sqrt{3})}{(x^2 + 9)^3}\end{aligned}$$

$$\begin{aligned}16. \quad f(x) &= \frac{x^3 - 1}{x^3 + 1} \\ f'(x) &= \frac{6x^2}{(x^3 + 1)^2} \\ f''(x) &= -\frac{24x(x^3 - \frac{1}{2})}{(x^3 + 1)^3}\end{aligned}$$

$$\begin{aligned}23. \quad f(x) &= x - 3x^{1/3} = x^{1/3}(x^{2/3} - 3) = \sqrt[3]{x}(\sqrt[3]{x} - \sqrt{3})(\sqrt[3]{x} + \sqrt{3}) \\ f'(x) &= \frac{x^{2/3} - 1}{x^{2/3}} = \frac{(\sqrt[3]{x})^2 - 1}{(\sqrt[3]{x})^2} = \frac{(\sqrt[3]{x} - 1)(\sqrt[3]{x} + 1)}{(\sqrt[3]{x})^2} \\ f''(x) &= \frac{2}{3\sqrt[3]{x^5}}\end{aligned}$$