# Math 12002 Exam V Review

Exam V will be given in class on Thursday, December 8, 2016. It will cover section 5.1-5.4, 5.6, and 5.8. This includes the following subjects (with a focus on parts 4 and 5, though these depend on parts 1, 2, and 3).

### 1 Inverse Functions

- Definition of a one-to-one and inverse function.
- Derivative of  $f^{-1}$  in terms of the derivative of f.
- Properties of inverses (cancellation).

# 2 Exponentials and Logarithms

- Definitions and properties, the number e, and the functions  $e^x$  and  $\ln x$ .
- Compute  $log_a x = y$  (find y given x and vice-versa).
- Solve equations involving logarithms and exponentials.
- Write  $a^x$  and  $\log_a x$  in terms of natural logarithms and exponentials.
- Simplify expressions using properties of logarithms.

### 3 Inverse Trigonometric Functions

- Definitions of  $\sin^{-1} x$ ,  $\cos^{-1} x$ , and  $\tan^{-1} x$  including domains and ranges.
- Compute values of these functions, know cancellation properties.

# 4 Calculus of Exponentials, Logarithms, and Inverse Trignometric Functions

- Limits involving  $a^x$ ,  $e^x$ ,  $\log_a x$ , and  $\ln x$  as well as combinations of such functions.
- Derivatives and integrals of functions involving  $a^x$ ,  $e^x$ ,  $\log_a x$ ,  $\ln x$ ,  $\frac{1}{x}$ ,  $[f(x)]^{g(x)}$ , inverse trig functions,  $\frac{1}{\sqrt{1-x^2}}$ ,  $\frac{1}{x^2+1}$ ,  $\frac{1}{x\sqrt{x^2-1}}$ , etc.
- Find equations of tangent lines to graphs of these functions.
- Curve sketching for these functions (increasing/decreasing, local max/min, concavity, inflection points).

# 5 Indeterminate Forms and l'Hopital's Rule

- Know when l'Hopital's Rule can be used and when it can't.
- Use l'Hospital's rule to compute limits.