## Important Properties:

- When a polynomial has four terms, common factors can sometimes by used to factor by grouping.
- Recall the formula for the difference of two squares:

$$x^2 - y^2 = (x - y)(x + y)$$

• It does not matter the order that you list the factors. For example,

$$(3x-2)(x+1) = (x+1)(3x-2).$$

• You can always check your answer by multiplication.

## Common Mistakes to Avoid:

- Recall that the sum of two squares does not factor.
- Sometimes the current order does not lead to a common factor. If this happens try rearranging the terms. Do not assume that this means that the expression cannot be factored.
- Be on the lookout for the difference of squares, the difference of cubes and the sum of cubes. Remember that these can be factored further.

## **PROBLEMS**

Factor completely.

1. 
$$2x^3 + 3x^2 - 8x - 12$$

$$2x^{3} + 3x^{2} - 8x - 12$$

$$x^{2}(2x+3) - 4(2x+3)$$

$$(2x+3)(x^{2}-4)$$

$$(2x+3)(x-2)(x+2)$$

$$2. \ 3x^3 - 2x^2 - 3x + 2$$

$$3x^{3} - 2x^{2} - 3x + 2$$

$$x^{2}(3x - 2) - (3x - 2)$$

$$(3x - 2)(x^{2} - 1)$$

$$(3x - 2)(x - 1)(x + 1)$$

3. 
$$12x^3 - 16x^2 + 3x - 4$$

$$\underbrace{\frac{12x^3 - 16x^2}{4x^2(3x - 4) + (3x - 4)}}_{(3x - 4)(4x^2 + 1)}$$

4. 
$$5x^3 - x^2 + 20x - 4$$

$$\underbrace{\frac{5x^3 - x^2}{x^2(5x - 1) + 4(5x - 1)}}_{(5x - 1)(x^2 + 4)}$$

5. 
$$24x^3 - 4x^2 - 6x + 1$$

$$\underbrace{24x^{3} - 4x^{2} - 6x + 1}_{4x^{2}(6x - 1) - (6x - 1)}_{(6x - 1)(4x^{2} - 1)}$$

$$\underbrace{(6x - 1)(2x - 1)(2x + 1)}_{(6x - 1)(2x + 1)}$$

6. 
$$18x^3 - 27x^2 + 8x - 12$$

$$\underbrace{\frac{18x^3 - 27x^2 + 8x - 12}{9x^2(2x - 3) + 4(2x - 3)}}_{(2x - 3)(9x^2 + 4)}$$

7. 
$$2x^3 + x^2 + 50x + 25$$

$$\underbrace{x^{2} + x^{2} + 50x + 25}_{x^{2}(2x+1) + 25(2x+1)}$$
$$\underbrace{(2x+1)(x^{2} + 25)}$$

8. 
$$10x^2 - 12y + 15x - 8xy$$

NOTE: The current order does not lead to a common factor. Therefore, we must first rearrange the terms.

$$10x^{2} - 12y + 15x - 8xy$$

$$10x^{2} - 8xy - 12y + 15x$$

$$2x(5x - 4y) + 3(-4y + 5x)$$

$$2x(5x - 4y) + 3(5x - 4y)$$

$$(5x - 4y)(2x + 3)$$

$$9. \ 10x^3 - 2x^2y^2 - 5xy + y^3$$

NOTE: The current order does not lead to a common factor. Therefore, we must first rearrange the terms.

$$\underbrace{\frac{10x^3 - 2x^2y^2 - 5xy + y^3}{10x^3 - 5xy} - \underbrace{2x^2y^2 + y^3}_{5x(2x^2 - y) - y^2(2x^2 - y)}}_{(2x^2 - y)(5x - y^2)}$$